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Year: 2013

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## Model-independent search for CP violation in $D^0$ to $K^-K^+\pi^-\pi^+$ and $D^0$ to $\pi^-\pi^+\pi^+\pi^-$ decays

LHCb Collaboration ; et al ; Bernet, R ; Müller, K ; Steinkamp, O ; Straumann, U ; Vollhardt, A

**Abstract:** A search for CP violation in the phase-space structures of  $D^0D^0$  and View the MathML source  $D^0$  decays to the final states  $K^-K^+\pi^-\pi^+$  and  $\pi^-\pi^+\pi^+\pi^-$  is presented. The search is carried out with a data set corresponding to an integrated luminosity of  $1.0\text{ fb}^{-1}$ – $11.0\text{ fb}^{-1}$  collected in 2011 by the LHCb experiment in pp collisions at a centre-of-mass energy of 7 TeV. For the  $K^-K^+\pi^-\pi^+$  final state, the four-body phase space is divided into 32 bins, each bin with approximately 1800 decays. The p-value under the hypothesis of no CP violation is 9.1%, and in no bin is a CP asymmetry greater than 6.5% observed. The phase space of the  $\pi^-\pi^+\pi^+\pi^-$  final state is partitioned into 128 bins, each bin with approximately 2500 decays. The p-value under the hypothesis of no CP violation is 41%, and in no bin is a CP asymmetry greater than 5.5% observed. All results are consistent with the hypothesis of no CP violation at the current sensitivity.

DOI: <https://doi.org/10.1016/j.physletb.2013.09.011>

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ZORA URL: <https://doi.org/10.5167/uzh-91534>

Journal Article

Originally published at:

LHCb Collaboration; et al; Bernet, R; Müller, K; Steinkamp, O; Straumann, U; Vollhardt, A (2013). Model-independent search for CP violation in  $D^0$  to  $K^-K^+\pi^-\pi^+$  and  $D^0$  to  $\pi^-\pi^+\pi^+\pi^-$  decays. *Physics Letters B*, 726(4-5):623-633.

DOI: <https://doi.org/10.1016/j.physletb.2013.09.011>



CERN-PH-EP-2013-151

LHCb-PAPER-2013-041

15 August 2013

# Model-independent search for $CP$ violation in $D^0 \rightarrow K^- K^+ \pi^- \pi^+$ and $D^0 \rightarrow \pi^- \pi^+ \pi^+ \pi^-$ decays

The LHCb collaboration<sup>†</sup>

## Abstract

A search for  $CP$  violation in the phase-space structures of  $D^0$  and  $\bar{D}^0$  decays to the final states  $K^- K^+ \pi^- \pi^+$  and  $\pi^- \pi^+ \pi^+ \pi^-$  is presented. The search is carried out with a data set corresponding to an integrated luminosity of  $1.0 \text{ fb}^{-1}$  collected in 2011 by the LHCb experiment in  $pp$  collisions at a centre-of-mass energy of 7 TeV. For the  $K^- K^+ \pi^- \pi^+$  final state, the four-body phase space is divided into 32 bins, each bin with approximately 1800 decays. The  $p$ -value under the hypothesis of no  $CP$  violation is 9.1%, and in no bin is a  $CP$  asymmetry greater than 6.5% observed. The phase space of the  $\pi^- \pi^+ \pi^+ \pi^-$  final state is partitioned into 128 bins, each bin with approximately 2500 decays. The  $p$ -value under the hypothesis of no  $CP$  violation is 41%, and in no bin is a  $CP$  asymmetry greater than 5.5% observed. All results are consistent with the hypothesis of no  $CP$  violation at the current sensitivity.

Submitted to Phys. Lett. B

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<sup>†</sup>Authors are listed on the following pages.



## LHCb collaboration

R. Aaij<sup>40</sup>, B. Adeva<sup>36</sup>, M. Adinolfi<sup>45</sup>, C. Adrover<sup>6</sup>, A. Affolder<sup>51</sup>, Z. Ajaltouni<sup>5</sup>, J. Albrecht<sup>9</sup>, F. Alessio<sup>37</sup>, M. Alexander<sup>50</sup>, S. Ali<sup>40</sup>, G. Alkhazov<sup>29</sup>, P. Alvarez Cartelle<sup>36</sup>, A.A. Alves Jr<sup>24,37</sup>, S. Amato<sup>2</sup>, S. Amerio<sup>21</sup>, Y. Amhis<sup>7</sup>, L. Anderlini<sup>17,f</sup>, J. Anderson<sup>39</sup>, R. Andreassen<sup>56</sup>, J.E. Andrews<sup>57</sup>, R.B. Appleby<sup>53</sup>, O. Aquines Gutierrez<sup>10</sup>, F. Archilli<sup>18</sup>, A. Artamonov<sup>34</sup>, M. Artuso<sup>58</sup>, E. Aslanides<sup>6</sup>, G. Auriemma<sup>24,m</sup>, M. Baalouch<sup>5</sup>, S. Bachmann<sup>11</sup>, J.J. Back<sup>47</sup>, C. Baesso<sup>59</sup>, V. Balagura<sup>30</sup>, W. Baldini<sup>16</sup>, R.J. Barlow<sup>53</sup>, C. Barschel<sup>37</sup>, S. Barsuk<sup>7</sup>, W. Barter<sup>46</sup>, Th. Bauer<sup>40</sup>, A. Bay<sup>38</sup>, J. Beddow<sup>50</sup>, F. Bedeschi<sup>22</sup>, I. Bediaga<sup>1</sup>, S. Belogurov<sup>30</sup>, K. Belous<sup>34</sup>, I. Belyaev<sup>30</sup>, E. Ben-Haim<sup>8</sup>, G. Bencivenni<sup>18</sup>, S. Benson<sup>49</sup>, J. Benton<sup>45</sup>, A. Berezhnoy<sup>31</sup>, R. Bernet<sup>39</sup>, M.-O. Bettler<sup>46</sup>, M. van Beuzekom<sup>40</sup>, A. Bien<sup>11</sup>, S. Bifani<sup>44</sup>, T. Bird<sup>53</sup>, A. Bizzeti<sup>17,h</sup>, P.M. Bjørnstad<sup>53</sup>, T. Blake<sup>37</sup>, F. Blanc<sup>38</sup>, J. Blouw<sup>11</sup>, S. Blusk<sup>58</sup>, V. Bocci<sup>24</sup>, A. Bondar<sup>33</sup>, N. Bondar<sup>29</sup>, W. Bonivento<sup>15</sup>, S. Borghi<sup>53</sup>, A. Borgia<sup>58</sup>, T.J.V. Bowcock<sup>51</sup>, E. Bowen<sup>39</sup>, C. Bozzi<sup>16</sup>, T. Brambach<sup>9</sup>, J. van den Brand<sup>41</sup>, J. Bressieux<sup>38</sup>, D. Brett<sup>53</sup>, M. Britsch<sup>10</sup>, T. Britton<sup>58</sup>, N.H. Brook<sup>45</sup>, H. Brown<sup>51</sup>, I. Burducea<sup>28</sup>, A. Bursche<sup>39</sup>, G. Busetto<sup>21,q</sup>, J. Buytaert<sup>37</sup>, S. Cadet<sup>15</sup>, O. Callot<sup>7</sup>, M. Calvi<sup>20,j</sup>, M. Calvo Gomez<sup>35,n</sup>, A. Camboni<sup>35</sup>, P. Campana<sup>18,37</sup>, D. Campora Perez<sup>37</sup>, A. Carbone<sup>14,c</sup>, G. Carboni<sup>23,k</sup>, R. Cardinale<sup>19,i</sup>, A. Cardini<sup>15</sup>, H. Carranza-Mejia<sup>49</sup>, L. Carson<sup>52</sup>, K. Carvalho Akiba<sup>2</sup>, G. Casse<sup>51</sup>, L. Castillo Garcia<sup>37</sup>, M. Cattaneo<sup>37</sup>, Ch. Cauet<sup>9</sup>, R. Cenci<sup>57</sup>, M. Charles<sup>54</sup>, Ph. Charpentier<sup>37</sup>, P. Chen<sup>3,38</sup>, N. Chiapolini<sup>39</sup>, M. Chrzasczcz<sup>25</sup>, K. Ciba<sup>37</sup>, X. Cid Vidal<sup>37</sup>, G. Ciezarek<sup>52</sup>, P.E.L. Clarke<sup>49</sup>, M. Clemencic<sup>37</sup>, H.V. Cliff<sup>46</sup>, J. Closier<sup>37</sup>, C. Coca<sup>28</sup>, V. Coco<sup>40</sup>, J. Cogan<sup>6</sup>, E. Cogneras<sup>5</sup>, P. Collins<sup>37</sup>, A. Comerma-Montells<sup>35</sup>, A. Contu<sup>15,37</sup>, A. Cook<sup>45</sup>, M. Coombes<sup>45</sup>, S. Coquereau<sup>8</sup>, G. Corti<sup>37</sup>, B. Couturier<sup>37</sup>, G.A. Cowan<sup>49</sup>, E. Cowie<sup>45</sup>, D.C. Craik<sup>47</sup>, S. Cunliffe<sup>52</sup>, R. Currie<sup>49</sup>, C. D'Ambrosio<sup>37</sup>, P. David<sup>8</sup>, P.N.Y. David<sup>40</sup>, A. Davis<sup>56</sup>, I. De Bonis<sup>4</sup>, K. De Bruyn<sup>40</sup>, S. De Capua<sup>53</sup>, M. De Cian<sup>11</sup>, J.M. De Miranda<sup>1</sup>, L. De Paula<sup>2</sup>, W. De Silva<sup>56</sup>, P. De Simone<sup>18</sup>, D. Decamp<sup>4</sup>, M. Deckenhoff<sup>9</sup>, L. Del Buono<sup>8</sup>, N. Déléage<sup>4</sup>, D. Derkach<sup>54</sup>, O. Deschamps<sup>5</sup>, F. Dettori<sup>41</sup>, A. Di Canto<sup>11</sup>, H. Dijkstra<sup>37</sup>, M. Dogaru<sup>28</sup>, S. Donleavy<sup>51</sup>, F. Dordei<sup>11</sup>, A. Dosil Suárez<sup>36</sup>, D. Dossett<sup>47</sup>, A. Dovbnya<sup>42</sup>, F. Dupertuis<sup>38</sup>, P. Durante<sup>37</sup>, R. Dzhelyadin<sup>34</sup>, A. Dziurda<sup>25</sup>, A. Dzyuba<sup>29</sup>, S. Easo<sup>48</sup>, U. Egede<sup>52</sup>, V. Egorychev<sup>30</sup>, S. Eidelman<sup>33</sup>, D. van Eijk<sup>40</sup>, S. Eisenhardt<sup>49</sup>, U. Eitschberger<sup>9</sup>, R. Ekelhof<sup>9</sup>, L. Eklund<sup>50,37</sup>, I. El Rifai<sup>5</sup>, Ch. Elsasser<sup>39</sup>, A. Falabella<sup>14,e</sup>, C. Färber<sup>11</sup>, G. Fardell<sup>49</sup>, C. Farinelli<sup>40</sup>, S. Farry<sup>51</sup>, D. Ferguson<sup>49</sup>, V. Fernandez Albor<sup>36</sup>, F. Ferreira Rodrigues<sup>1</sup>, M. Ferro-Luzzi<sup>37</sup>, S. Filippov<sup>32</sup>, M. Fiore<sup>16</sup>, C. Fitzpatrick<sup>37</sup>, M. Fontana<sup>10</sup>, F. Fontanelli<sup>19,i</sup>, R. Forty<sup>37</sup>, O. Francisco<sup>2</sup>, M. Frank<sup>37</sup>, C. Frei<sup>37</sup>, M. Frosini<sup>17,f</sup>, S. Furcas<sup>20</sup>, E. Furfaro<sup>23,k</sup>, A. Gallas Torreira<sup>36</sup>, D. Galli<sup>14,c</sup>, M. Gandelman<sup>2</sup>, P. Gandini<sup>58</sup>, Y. Gao<sup>3</sup>, J. Garofoli<sup>58</sup>, P. Garosi<sup>53</sup>, J. Garra Tico<sup>46</sup>, L. Garrido<sup>35</sup>, C. Gaspar<sup>37</sup>, R. Gauld<sup>54</sup>, E. Gersabeck<sup>11</sup>, M. Gersabeck<sup>53</sup>, T. Gershon<sup>47,37</sup>, Ph. Ghez<sup>4</sup>, V. Gibson<sup>46</sup>, L. Giubega<sup>28</sup>, V.V. Gligorov<sup>37</sup>, C. Göbel<sup>59</sup>, D. Golubkov<sup>30</sup>, A. Golutvin<sup>52,30,37</sup>, A. Gomes<sup>2</sup>, P. Gorbounov<sup>30,37</sup>, H. Gordon<sup>37</sup>, C. Gotti<sup>20</sup>, M. Grabalosa Gándara<sup>5</sup>, R. Graciani Diaz<sup>35</sup>, L.A. Granado Cardoso<sup>37</sup>, E. Graugés<sup>35</sup>, G. Graziani<sup>17</sup>, A. Grecu<sup>28</sup>, E. Greening<sup>54</sup>, S. Gregson<sup>46</sup>, P. Griffith<sup>44</sup>, O. Grünberg<sup>60</sup>, B. Gui<sup>58</sup>, E. Gushchin<sup>32</sup>, Yu. Guz<sup>34,37</sup>, T. Gys<sup>37</sup>, C. Hadjivasiliou<sup>58</sup>, G. Haefeli<sup>38</sup>, C. Haen<sup>37</sup>, S.C. Haines<sup>46</sup>, S. Hall<sup>52</sup>, B. Hamilton<sup>57</sup>, T. Hampson<sup>45</sup>, S. Hansmann-Menzemer<sup>11</sup>, N. Harnew<sup>54</sup>, S.T. Harnew<sup>45</sup>, J. Harrison<sup>53</sup>, T. Hartmann<sup>60</sup>, J. He<sup>37</sup>, T. Head<sup>37</sup>, V. Heijne<sup>40</sup>, K. Hennessy<sup>51</sup>, P. Henrard<sup>5</sup>, J.A. Hernando Morata<sup>36</sup>, E. van Herwijnen<sup>37</sup>, M. Hess<sup>60</sup>, A. Hicheur<sup>1</sup>, E. Hicks<sup>51</sup>, D. Hill<sup>54</sup>, M. Hoballah<sup>5</sup>, C. Hombach<sup>53</sup>, P. Hopchev<sup>4</sup>, W. Hulsbergen<sup>40</sup>, P. Hunt<sup>54</sup>, T. Huse<sup>51</sup>, N. Hussain<sup>54</sup>, D. Hutchcroft<sup>51</sup>,

D. Hynds<sup>50</sup>, V. Iakovenko<sup>43</sup>, M. Idzik<sup>26</sup>, P. Ilten<sup>12</sup>, R. Jacobsson<sup>37</sup>, A. Jaeger<sup>11</sup>, E. Jans<sup>40</sup>,  
P. Jatón<sup>38</sup>, A. Jawahery<sup>57</sup>, F. Jing<sup>3</sup>, M. John<sup>54</sup>, D. Johnson<sup>54</sup>, C.R. Jones<sup>46</sup>, C. Joram<sup>37</sup>,  
B. Jost<sup>37</sup>, M. Kaballo<sup>9</sup>, S. Kandybei<sup>42</sup>, W. Kanso<sup>6</sup>, M. Karacson<sup>37</sup>, T.M. Karbach<sup>37</sup>,  
I.R. Kenyon<sup>44</sup>, T. Ketel<sup>41</sup>, A. Keune<sup>38</sup>, B. Khanji<sup>20</sup>, O. Kochebina<sup>7</sup>, I. Komarov<sup>38</sup>,  
R.F. Koopman<sup>41</sup>, P. Koppenburg<sup>40</sup>, M. Korolev<sup>31</sup>, A. Kozlinskiy<sup>40</sup>, L. Kravchuk<sup>32</sup>, K. Kreplin<sup>11</sup>,  
M. Kreps<sup>47</sup>, G. Krocker<sup>11</sup>, P. Krokovny<sup>33</sup>, F. Kruse<sup>9</sup>, M. Kucharczyk<sup>20,25,j</sup>, V. Kudryavtsev<sup>33</sup>,  
K. Kurek<sup>27</sup>, T. Kvaratskheliya<sup>30,37</sup>, V.N. La Thi<sup>38</sup>, D. Lacarrere<sup>37</sup>, G. Lafferty<sup>53</sup>, A. Lai<sup>15</sup>,  
D. Lambert<sup>49</sup>, R.W. Lambert<sup>41</sup>, E. Lanciotti<sup>37</sup>, G. Lanfranchi<sup>18</sup>, C. Langenbruch<sup>37</sup>,  
T. Latham<sup>47</sup>, C. Lazzeroni<sup>44</sup>, R. Le Gac<sup>6</sup>, J. van Leerdam<sup>40</sup>, J.-P. Lees<sup>4</sup>, R. Lefèvre<sup>5</sup>,  
A. Leflat<sup>31</sup>, J. Lefrançois<sup>7</sup>, S. Leo<sup>22</sup>, O. Leroy<sup>6</sup>, T. Lesiak<sup>25</sup>, B. Leverington<sup>11</sup>, Y. Li<sup>3</sup>,  
L. Li Gioi<sup>5</sup>, M. Liles<sup>51</sup>, R. Lindner<sup>37</sup>, C. Linn<sup>11</sup>, B. Liu<sup>3</sup>, G. Liu<sup>37</sup>, S. Lohn<sup>37</sup>, I. Longstaff<sup>50</sup>,  
J.H. Lopes<sup>2</sup>, N. Lopez-March<sup>38</sup>, H. Lu<sup>3</sup>, D. Lucchesi<sup>21,q</sup>, J. Luisier<sup>38</sup>, H. Luo<sup>49</sup>, F. Machefert<sup>7</sup>,  
I.V. Machikhiliyan<sup>4,30</sup>, F. Maciuc<sup>28</sup>, O. Maev<sup>29,37</sup>, S. Malde<sup>54</sup>, G. Manca<sup>15,d</sup>, G. Mancinelli<sup>6</sup>,  
J. Maratas<sup>5</sup>, U. Marconi<sup>14</sup>, P. Marino<sup>22,s</sup>, R. Märki<sup>38</sup>, J. Marks<sup>11</sup>, G. Martellotti<sup>24</sup>, A. Martens<sup>8</sup>,  
A. Martín Sánchez<sup>7</sup>, M. Martinelli<sup>40</sup>, D. Martinez Santos<sup>41</sup>, D. Martins Tostes<sup>2</sup>, A. Martynov<sup>31</sup>,  
A. Massafferri<sup>1</sup>, R. Matev<sup>37</sup>, Z. Mathe<sup>37</sup>, C. Matteuzzi<sup>20</sup>, E. Maurice<sup>6</sup>, A. Mazurov<sup>16,32,37,e</sup>,  
J. McCarthy<sup>44</sup>, A. McNab<sup>53</sup>, R. McNulty<sup>12</sup>, B. McSkelly<sup>51</sup>, B. Meadows<sup>56,54</sup>, F. Meier<sup>9</sup>,  
M. Meissner<sup>11</sup>, M. Merk<sup>40</sup>, D.A. Milanese<sup>8</sup>, M.-N. Minard<sup>4</sup>, J. Molina Rodriguez<sup>59</sup>, S. Monteil<sup>5</sup>,  
D. Moran<sup>53</sup>, P. Morawski<sup>25</sup>, A. Mordà<sup>6</sup>, M.J. Morello<sup>22,s</sup>, R. Mountain<sup>58</sup>, I. Mous<sup>40</sup>,  
F. Muheim<sup>49</sup>, K. Müller<sup>39</sup>, R. Muresan<sup>28</sup>, B. Muryn<sup>26</sup>, B. Muster<sup>38</sup>, P. Naik<sup>45</sup>, T. Nakada<sup>38</sup>,  
R. Nandakumar<sup>48</sup>, I. Nasteva<sup>1</sup>, M. Needham<sup>49</sup>, S. Neubert<sup>37</sup>, N. Neufeld<sup>37</sup>, A.D. Nguyen<sup>38</sup>,  
T.D. Nguyen<sup>38</sup>, C. Nguyen-Mau<sup>38,o</sup>, M. Nicol<sup>7</sup>, V. Niess<sup>5</sup>, R. Niet<sup>9</sup>, N. Nikitin<sup>31</sup>, T. Nikodem<sup>11</sup>,  
A. Nomerotski<sup>54</sup>, A. Novoselov<sup>34</sup>, A. Oblakowska-Mucha<sup>26</sup>, V. Obraztsov<sup>34</sup>, S. Oggero<sup>40</sup>,  
S. Ogilvy<sup>50</sup>, O. Okhrimenko<sup>43</sup>, R. Oldeman<sup>15,d</sup>, M. Orlandea<sup>28</sup>, J.M. Otalora Goicochea<sup>2</sup>,  
P. Owen<sup>52</sup>, A. Oyanguren<sup>35</sup>, B.K. Pal<sup>58</sup>, A. Palano<sup>13,b</sup>, T. Palczewski<sup>27</sup>, M. Palutan<sup>18</sup>,  
J. Panman<sup>37</sup>, A. Papanestis<sup>48</sup>, M. Pappagallo<sup>50</sup>, C. Parkes<sup>53</sup>, C.J. Parkinson<sup>52</sup>, G. Passaleva<sup>17</sup>,  
G.D. Patel<sup>51</sup>, M. Patel<sup>52</sup>, G.N. Patrick<sup>48</sup>, C. Patrignani<sup>19,i</sup>, C. Pavel-Nicorescu<sup>28</sup>,  
A. Pazos Alvarez<sup>36</sup>, A. Pellegrino<sup>40</sup>, G. Penso<sup>24,l</sup>, M. Pepe Altarelli<sup>37</sup>, S. Perazzini<sup>14,c</sup>,  
E. Perez Trigo<sup>36</sup>, A. Pérez-Calero Yzquierdo<sup>35</sup>, P. Perret<sup>5</sup>, M. Perrin-Terrin<sup>6</sup>, L. Pescatore<sup>44</sup>,  
E. Pesen<sup>61</sup>, K. Petridis<sup>52</sup>, A. Petrolini<sup>19,i</sup>, A. Phan<sup>58</sup>, E. Picatoste Olloqui<sup>35</sup>, B. Pietrzyk<sup>4</sup>,  
T. Pilar<sup>47</sup>, D. Pinci<sup>24</sup>, S. Playfer<sup>49</sup>, M. Plo Casasus<sup>36</sup>, F. Polci<sup>8</sup>, G. Polok<sup>25</sup>, A. Poluektov<sup>47,33</sup>,  
E. Polcarpo<sup>2</sup>, A. Popov<sup>34</sup>, D. Popov<sup>10</sup>, B. Popovici<sup>28</sup>, C. Potterat<sup>35</sup>, A. Powell<sup>54</sup>,  
J. Prisciandaro<sup>38</sup>, A. Pritchard<sup>51</sup>, C. Prouve<sup>7</sup>, V. Pugatch<sup>43</sup>, A. Puig Navarro<sup>38</sup>, G. Punzi<sup>22,r</sup>,  
W. Qian<sup>4</sup>, J.H. Rademacker<sup>45</sup>, B. Rakotomiamanana<sup>38</sup>, M.S. Rangel<sup>2</sup>, I. Raniuk<sup>42</sup>,  
N. Rauschmayr<sup>37</sup>, G. Raven<sup>41</sup>, S. Redford<sup>54</sup>, M.M. Reid<sup>47</sup>, A.C. dos Reis<sup>1</sup>, S. Ricciardi<sup>48</sup>,  
A. Richards<sup>52</sup>, K. Rinnert<sup>51</sup>, V. Rives Molina<sup>35</sup>, D.A. Roa Romero<sup>5</sup>, P. Robbe<sup>7</sup>, D.A. Roberts<sup>57</sup>,  
E. Rodrigues<sup>53</sup>, P. Rodriguez Perez<sup>36</sup>, S. Roiser<sup>37</sup>, V. Romanovsky<sup>34</sup>, A. Romero Vidal<sup>36</sup>,  
J. Rouvinet<sup>38</sup>, T. Ruf<sup>37</sup>, F. Ruffini<sup>22</sup>, H. Ruiz<sup>35</sup>, P. Ruiz Valls<sup>35</sup>, G. Sabatino<sup>24,k</sup>,  
J.J. Saborido Silva<sup>36</sup>, N. Sagidova<sup>29</sup>, P. Sail<sup>50</sup>, B. Saitta<sup>15,d</sup>, V. Salustino Guimaraes<sup>2</sup>,  
B. Sanmartin Sedes<sup>36</sup>, M. Sannino<sup>19,i</sup>, R. Santacesaria<sup>24</sup>, C. Santamarina Rios<sup>36</sup>,  
E. Santovetti<sup>23,k</sup>, M. Sapunov<sup>6</sup>, A. Sarti<sup>18,l</sup>, C. Satriano<sup>24,m</sup>, A. Satta<sup>23</sup>, M. Savrie<sup>16,e</sup>,  
D. Savrina<sup>30,31</sup>, P. Schaack<sup>52</sup>, M. Schiller<sup>41</sup>, H. Schindler<sup>37</sup>, M. Schlupp<sup>9</sup>, M. Schmelling<sup>10</sup>,  
B. Schmidt<sup>37</sup>, O. Schneider<sup>38</sup>, A. Schopper<sup>37</sup>, M.-H. Schune<sup>7</sup>, R. Schwemmer<sup>37</sup>, B. Sciascia<sup>18</sup>,  
A. Sciubba<sup>24</sup>, M. Seco<sup>36</sup>, A. Semennikov<sup>30</sup>, K. Senderowska<sup>26</sup>, I. Sepp<sup>52</sup>, N. Serra<sup>39</sup>, J. Serrano<sup>6</sup>,  
P. Seyfert<sup>11</sup>, M. Shapkin<sup>34</sup>, I. Shapoval<sup>16,42</sup>, P. Shatalov<sup>30</sup>, Y. Shcheglov<sup>29</sup>, T. Shears<sup>51,37</sup>,  
L. Shekhtman<sup>33</sup>, O. Shevchenko<sup>42</sup>, V. Shevchenko<sup>30</sup>, A. Shires<sup>9</sup>, R. Silva Coutinho<sup>47</sup>,

M. Sirendi<sup>46</sup>, N. Skidmore<sup>45</sup>, T. Skwarnicki<sup>58</sup>, N.A. Smith<sup>51</sup>, E. Smith<sup>54,48</sup>, J. Smith<sup>46</sup>,  
M. Smith<sup>53</sup>, M.D. Sokoloff<sup>56</sup>, F.J.P. Soler<sup>50</sup>, F. Soomro<sup>38</sup>, D. Souza<sup>45</sup>, B. Souza De Paula<sup>2</sup>,  
B. Spaan<sup>9</sup>, A. Sparkes<sup>49</sup>, P. Spradlin<sup>50</sup>, F. Stagni<sup>37</sup>, S. Stahl<sup>11</sup>, O. Steinkamp<sup>39</sup>, S. Stevenson<sup>54</sup>,  
S. Stoica<sup>28</sup>, S. Stone<sup>58</sup>, B. Storaci<sup>39</sup>, M. Straticiuc<sup>28</sup>, U. Straumann<sup>39</sup>, V.K. Subbiah<sup>37</sup>, L. Sun<sup>56</sup>,  
S. Swientek<sup>9</sup>, V. Syropoulos<sup>41</sup>, M. Szczekowski<sup>27</sup>, P. Szczypka<sup>38,37</sup>, T. Szumlak<sup>26</sup>,  
S. T'Jampens<sup>4</sup>, M. Teklishyn<sup>7</sup>, E. Teodorescu<sup>28</sup>, F. Teubert<sup>37</sup>, C. Thomas<sup>54</sup>, E. Thomas<sup>37</sup>,  
J. van Tilburg<sup>11</sup>, V. Tisserand<sup>4</sup>, M. Tobin<sup>38</sup>, S. Tolk<sup>41</sup>, D. Tonelli<sup>37</sup>, S. Topp-Joergensen<sup>54</sup>,  
N. Tori<sup>54</sup>, E. Tournefier<sup>4,52</sup>, S. Tourneur<sup>38</sup>, M.T. Tran<sup>38</sup>, M. Tresch<sup>39</sup>, A. Tsaregorodtsev<sup>6</sup>,  
P. Tsopelas<sup>40</sup>, N. Tuning<sup>40</sup>, M. Ubeda Garcia<sup>37</sup>, A. Ukleja<sup>27</sup>, D. Urner<sup>53</sup>, A. Ustyuzhanin<sup>52,p</sup>,  
U. Uwer<sup>11</sup>, V. Vagnoni<sup>14</sup>, G. Valenti<sup>14</sup>, A. Vallier<sup>7</sup>, M. Van Dijk<sup>45</sup>, R. Vazquez Gomez<sup>18</sup>,  
P. Vazquez Regueiro<sup>36</sup>, C. Vázquez Sierra<sup>36</sup>, S. Vecchi<sup>16</sup>, J.J. Velthuis<sup>45</sup>, M. Veltri<sup>17,g</sup>,  
G. Veneziano<sup>38</sup>, M. Vesterinen<sup>37</sup>, B. Viaud<sup>7</sup>, D. Vieira<sup>2</sup>, X. Vilasis-Cardona<sup>35,n</sup>, A. Vollhardt<sup>39</sup>,  
D. Volyanskyy<sup>10</sup>, D. Voong<sup>45</sup>, A. Vorobyev<sup>29</sup>, V. Vorobyev<sup>33</sup>, C. Voß<sup>60</sup>, H. Voss<sup>10</sup>, R. Waldi<sup>60</sup>,  
C. Wallace<sup>47</sup>, R. Wallace<sup>12</sup>, S. Wandernoth<sup>11</sup>, J. Wang<sup>58</sup>, D.R. Ward<sup>46</sup>, N.K. Watson<sup>44</sup>,  
A.D. Webber<sup>53</sup>, D. Websdale<sup>52</sup>, M. Whitehead<sup>47</sup>, J. Wicht<sup>37</sup>, J. Wiechczynski<sup>25</sup>, D. Wiedner<sup>11</sup>,  
L. Wiggers<sup>40</sup>, G. Wilkinson<sup>54</sup>, M.P. Williams<sup>47,48</sup>, M. Williams<sup>55</sup>, F.F. Wilson<sup>48</sup>,  
J. Wimberley<sup>57</sup>, J. Wishahi<sup>9</sup>, W. Wislicki<sup>27</sup>, M. Witek<sup>25</sup>, S.A. Wotton<sup>46</sup>, S. Wright<sup>46</sup>, S. Wu<sup>3</sup>,  
K. Wyllie<sup>37</sup>, Y. Xie<sup>49,37</sup>, Z. Xing<sup>58</sup>, Z. Yang<sup>3</sup>, R. Young<sup>49</sup>, X. Yuan<sup>3</sup>, O. Yushchenko<sup>34</sup>,  
M. Zangoli<sup>14</sup>, M. Zavertyaev<sup>10,a</sup>, F. Zhang<sup>3</sup>, L. Zhang<sup>58</sup>, W.C. Zhang<sup>12</sup>, Y. Zhang<sup>3</sup>,  
A. Zhelezov<sup>11</sup>, A. Zhokhov<sup>30</sup>, L. Zhong<sup>3</sup>, A. Zvyagin<sup>37</sup>.

<sup>1</sup>Centro Brasileiro de Pesquisas Físicas (CBPF), Rio de Janeiro, Brazil

<sup>2</sup>Universidade Federal do Rio de Janeiro (UFRJ), Rio de Janeiro, Brazil

<sup>3</sup>Center for High Energy Physics, Tsinghua University, Beijing, China

<sup>4</sup>LAPP, Université de Savoie, CNRS/IN2P3, Annecy-Le-Vieux, France

<sup>5</sup>Clermont Université, Université Blaise Pascal, CNRS/IN2P3, LPC, Clermont-Ferrand, France

<sup>6</sup>CPPM, Aix-Marseille Université, CNRS/IN2P3, Marseille, France

<sup>7</sup>LAL, Université Paris-Sud, CNRS/IN2P3, Orsay, France

<sup>8</sup>LPNHE, Université Pierre et Marie Curie, Université Paris Diderot, CNRS/IN2P3, Paris, France

<sup>9</sup>Fakultät Physik, Technische Universität Dortmund, Dortmund, Germany

<sup>10</sup>Max-Planck-Institut für Kernphysik (MPIK), Heidelberg, Germany

<sup>11</sup>Physikalisches Institut, Ruprecht-Karls-Universität Heidelberg, Heidelberg, Germany

<sup>12</sup>School of Physics, University College Dublin, Dublin, Ireland

<sup>13</sup>Sezione INFN di Bari, Bari, Italy

<sup>14</sup>Sezione INFN di Bologna, Bologna, Italy

<sup>15</sup>Sezione INFN di Cagliari, Cagliari, Italy

<sup>16</sup>Sezione INFN di Ferrara, Ferrara, Italy

<sup>17</sup>Sezione INFN di Firenze, Firenze, Italy

<sup>18</sup>Laboratori Nazionali dell'INFN di Frascati, Frascati, Italy

<sup>19</sup>Sezione INFN di Genova, Genova, Italy

<sup>20</sup>Sezione INFN di Milano Bicocca, Milano, Italy

<sup>21</sup>Sezione INFN di Padova, Padova, Italy

<sup>22</sup>Sezione INFN di Pisa, Pisa, Italy

<sup>23</sup>Sezione INFN di Roma Tor Vergata, Roma, Italy

<sup>24</sup>Sezione INFN di Roma La Sapienza, Roma, Italy

<sup>25</sup>Henryk Niewodniczanski Institute of Nuclear Physics Polish Academy of Sciences, Kraków, Poland

<sup>26</sup>AGH - University of Science and Technology, Faculty of Physics and Applied Computer Science, Kraków, Poland

<sup>27</sup>National Center for Nuclear Research (NCBJ), Warsaw, Poland

- <sup>28</sup> Horia Hulubei National Institute of Physics and Nuclear Engineering, Bucharest-Magurele, Romania
- <sup>29</sup> Petersburg Nuclear Physics Institute (PNPI), Gatchina, Russia
- <sup>30</sup> Institute of Theoretical and Experimental Physics (ITEP), Moscow, Russia
- <sup>31</sup> Institute of Nuclear Physics, Moscow State University (SINP MSU), Moscow, Russia
- <sup>32</sup> Institute for Nuclear Research of the Russian Academy of Sciences (INR RAN), Moscow, Russia
- <sup>33</sup> Budker Institute of Nuclear Physics (SB RAS) and Novosibirsk State University, Novosibirsk, Russia
- <sup>34</sup> Institute for High Energy Physics (IHEP), Protvino, Russia
- <sup>35</sup> Universitat de Barcelona, Barcelona, Spain
- <sup>36</sup> Universidad de Santiago de Compostela, Santiago de Compostela, Spain
- <sup>37</sup> European Organization for Nuclear Research (CERN), Geneva, Switzerland
- <sup>38</sup> Ecole Polytechnique Fédérale de Lausanne (EPFL), Lausanne, Switzerland
- <sup>39</sup> Physik-Institut, Universität Zürich, Zürich, Switzerland
- <sup>40</sup> Nikhef National Institute for Subatomic Physics, Amsterdam, The Netherlands
- <sup>41</sup> Nikhef National Institute for Subatomic Physics and VU University Amsterdam, Amsterdam, The Netherlands
- <sup>42</sup> NSC Kharkiv Institute of Physics and Technology (NSC KIPT), Kharkiv, Ukraine
- <sup>43</sup> Institute for Nuclear Research of the National Academy of Sciences (KINR), Kyiv, Ukraine
- <sup>44</sup> University of Birmingham, Birmingham, United Kingdom
- <sup>45</sup> H.H. Wills Physics Laboratory, University of Bristol, Bristol, United Kingdom
- <sup>46</sup> Cavendish Laboratory, University of Cambridge, Cambridge, United Kingdom
- <sup>47</sup> Department of Physics, University of Warwick, Coventry, United Kingdom
- <sup>48</sup> STFC Rutherford Appleton Laboratory, Didcot, United Kingdom
- <sup>49</sup> School of Physics and Astronomy, University of Edinburgh, Edinburgh, United Kingdom
- <sup>50</sup> School of Physics and Astronomy, University of Glasgow, Glasgow, United Kingdom
- <sup>51</sup> Oliver Lodge Laboratory, University of Liverpool, Liverpool, United Kingdom
- <sup>52</sup> Imperial College London, London, United Kingdom
- <sup>53</sup> School of Physics and Astronomy, University of Manchester, Manchester, United Kingdom
- <sup>54</sup> Department of Physics, University of Oxford, Oxford, United Kingdom
- <sup>55</sup> Massachusetts Institute of Technology, Cambridge, MA, United States
- <sup>56</sup> University of Cincinnati, Cincinnati, OH, United States
- <sup>57</sup> University of Maryland, College Park, MD, United States
- <sup>58</sup> Syracuse University, Syracuse, NY, United States
- <sup>59</sup> Pontifícia Universidade Católica do Rio de Janeiro (PUC-Rio), Rio de Janeiro, Brazil, associated to <sup>2</sup>
- <sup>60</sup> Institut für Physik, Universität Rostock, Rostock, Germany, associated to <sup>11</sup>
- <sup>61</sup> Celal Bayar University, Manisa, Turkey, associated to <sup>37</sup>

<sup>a</sup> P.N. Lebedev Physical Institute, Russian Academy of Science (LPI RAS), Moscow, Russia

<sup>b</sup> Università di Bari, Bari, Italy

<sup>c</sup> Università di Bologna, Bologna, Italy

<sup>d</sup> Università di Cagliari, Cagliari, Italy

<sup>e</sup> Università di Ferrara, Ferrara, Italy

<sup>f</sup> Università di Firenze, Firenze, Italy

<sup>g</sup> Università di Urbino, Urbino, Italy

<sup>h</sup> Università di Modena e Reggio Emilia, Modena, Italy

<sup>i</sup> Università di Genova, Genova, Italy

<sup>j</sup> Università di Milano Bicocca, Milano, Italy

<sup>k</sup> Università di Roma Tor Vergata, Roma, Italy

<sup>l</sup> Università di Roma La Sapienza, Roma, Italy

<sup>m</sup> Università della Basilicata, Potenza, Italy

<sup>n</sup> LIFAELS, La Salle, Universitat Ramon Llull, Barcelona, Spain

<sup>o</sup> Hanoi University of Science, Hanoi, Viet Nam

<sup>p</sup> Institute of Physics and Technology, Moscow, Russia

<sup>q</sup>*Università di Padova, Padova, Italy*

<sup>r</sup>*Università di Pisa, Pisa, Italy*

<sup>s</sup>*Scuola Normale Superiore, Pisa, Italy*



# 1 Introduction

Standard Model predictions for the magnitude of  $CP$  violation (CPV) in charm meson decays are generally of  $\mathcal{O}(10^{-3})$  [1, 2], although values up to  $\mathcal{O}(10^{-2})$  cannot be ruled out [3, 4]. The size of CPV can be significantly enhanced in new physics models [5, 6], making charm transitions a promising area to search for new physics. Previous searches for CPV in charm decays caused a large interest in the community [7–9] and justify detailed searches for CPV in many different final states. Direct CPV can occur when at least two amplitudes interfere with strong and weak phases that each differ from one another. Singly-Cabibbo-suppressed charm hadron decays, where both tree processes and electroweak loop processes can contribute, are promising channels with which to search for CPV. The rich structure of interfering amplitudes makes four-body decays ideal to perform such searches.

The phase-space structures of the  $D^0 \rightarrow K^- K^+ \pi^- \pi^+$  and  $D^0 \rightarrow \pi^- \pi^+ \pi^+ \pi^-$  decays<sup>1</sup> are investigated for localised CPV in a manner that is independent of an amplitude model of the  $D^0$  meson decay. The Cabibbo-favoured  $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$  decay, where direct CPV can not occur in the Standard Model, is used as a control channel. A model-dependent search for CPV in  $D^0 \rightarrow K^- K^+ \pi^- \pi^+$  was previously carried out by the CLEO collaboration [10] with a data set of approximately 3000 signal decays, where no evidence for CPV was observed. This analysis is carried out on a data set of approximately  $5.7 \times 10^4$   $D^0 \rightarrow K^- K^+ \pi^- \pi^+$  decays and  $3.3 \times 10^5$   $D^0 \rightarrow \pi^- \pi^+ \pi^+ \pi^-$  decays. The data set is based on an integrated luminosity of  $1.0 \text{ fb}^{-1}$  of  $pp$  collisions with a centre-of-mass energy of 7 TeV, recorded by the LHCb experiment during 2011. The analysis is based on  $D^0$  mesons produced in  $D^{*+} \rightarrow D^0 \pi^+$  decays. The charge of the soft pion ( $\pi^+$ ) identifies the flavour of the meson at production. The phase space is partitioned into  $N_{\text{bins}}$  bins, and the significance of the difference in population between  $CP$  conjugate decays for each bin is calculated as

$$S_{CP}^i = \frac{N_i(D^0) - \alpha N_i(\bar{D}^0)}{\sqrt{\alpha (\sigma_i^2(D^0) + \sigma_i^2(\bar{D}^0))}}, \quad \alpha = \frac{\sum_i N_i(D^0)}{\sum_i N_i(\bar{D}^0)}, \quad (1)$$

where  $N_i$  is the number of signal decays in bin  $i$ , and  $\sigma_i$  is the associated uncertainty in the number of signal decays in bin  $i$  [11]. The normalisation constant  $\alpha$  removes global production and detection differences between  $D^{*+}$  and  $D^{*-}$  decays.

In the absence of any asymmetry,  $S_{CP}$  is Gaussian distributed with a mean of zero and a width of one. A significant variation from a unit Gaussian distribution indicates the presence of an asymmetry. The sum of squared  $S_{CP}$  values is a  $\chi^2$  statistic,

$$\chi^2 = \sum_i (S_{CP}^i)^2,$$

with  $N_{\text{bins}} - 1$  degrees of freedom, from which a  $p$ -value is calculated. Previous analyses of three-body  $D$  meson decays have employed similar analysis techniques [12, 13].

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<sup>1</sup>Unless otherwise specified, inclusion of charge-conjugate processes is implied.

## 2 Detector

The LHCb detector [14] is a single-arm forward spectrometer covering the pseudorapidity range  $2 < \eta < 5$ , designed for the study of particles containing  $b$  or  $c$  quarks. The detector includes a high-precision tracking system consisting of a silicon-strip vertex detector surrounding the  $pp$  interaction region, a large-area silicon-strip detector located upstream of a dipole magnet with a vertically oriented magnetic field and bending power of about 4 Tm, and three stations of silicon-strip detectors and straw drift tubes placed downstream. To alleviate the impact of charged particle-antiparticle detection asymmetries, the magnetic field polarity is switched regularly, and data are taken in each polarity. The two magnet polarities are henceforth referred to as “magnet up” and “magnet down”. The combined tracking system provides momentum measurement with relative uncertainty that varies from 0.4% at 5 GeV/ $c$  to 0.6% at 100 GeV/ $c$ , and impact parameter resolution of 20  $\mu\text{m}$  for tracks with high transverse momentum. Charged hadrons are identified with two ring-imaging Cherenkov (RICH) detectors [15]. Photon, electron, and hadron candidates are identified by a calorimeter system consisting of scintillating-pad and preshower detectors, an electromagnetic calorimeter, and a hadronic calorimeter. Muons are identified by a system composed of alternating layers of iron and multiwire proportional chambers. The trigger consists of a hardware stage, based on information from the calorimeter and muon systems, followed by a software stage [16]. Events are required to pass both hardware and software trigger levels. The software trigger optimised for the reconstruction of four-body hadronic charm decays requires a four-track secondary vertex with a scalar sum of the transverse momenta,  $p_{\text{T}}$ , of the tracks greater than 2 GeV/ $c$ . At least two tracks are required to have  $p_{\text{T}} > 500$  MeV/ $c$  and momentum,  $p$ , greater than 5 GeV/ $c$ . The remaining two tracks are required to have  $p_{\text{T}} > 250$  MeV/ $c$  and  $p > 2$  GeV/ $c$ . A requirement is also imposed on the  $\chi^2$  of the impact parameter ( $\chi_{\text{IP}}^2$ ) of the remaining two tracks with respect to any primary interaction to be greater than 10, where  $\chi_{\text{IP}}^2$  is defined as the difference in  $\chi^2$  of a given primary vertex reconstructed with and without the considered track.

## 3 Selection

Candidate  $D^0$  decays are reconstructed from combinations of pion and kaon candidate tracks. The  $D^0$  candidates are required to have  $p_{\text{T}} > 3$  GeV/ $c$ . The  $D^0$  decay products are required to have  $p > 3$  GeV/ $c$  and  $p_{\text{T}} > 350$  MeV/ $c$ . The  $D^0$  decay products are required to form a vertex with a  $\chi^2$  per degree of freedom ( $\chi^2/\text{ndf}$ ) less than 10 and a maximum distance of closest approach between any pair of  $D^0$  decay products less than 0.12 mm. The RICH system is used to distinguish between kaons and pions when reconstructing the  $D^0$  candidate. The  $D^{*+}$  candidates are reconstructed from  $D^0$  candidates combined with a track with  $p_{\text{T}} > 120$  MeV/ $c$ . Decays are selected with candidate  $D^0$  mass,  $m(hhhh)$ , of  $1804 < m(hhhh) < 1924$  MeV/ $c^2$ , where the notation  $m(hhhh)$  denotes the invariant mass of any of the considered final states; specific notations are used where appropriate. The difference,  $\Delta m$ , in the reconstructed  $D^{*+}$  mass and  $m(hhhh)$  for candidate decays is required to be  $137.9 < \Delta m < 155.0$  MeV/ $c^2$ . The decay vertex of the  $D^*$  is constrained to

coincide with the primary vertex [17].

Differences in  $D^{*+}$  and  $D^{*-}$  meson production and detection efficiencies can introduce asymmetries across the phase-space distributions of the  $D^0$  decay. To ensure that the soft pion is detected in the central region of the detector, fiducial cuts on its momentum are applied, as in Ref. [9]. The  $D^0$  and  $\bar{D}^0$  candidates are weighted by removing events so that they have same transverse momentum and pseudorapidity distributions. To further cancel detection asymmetries the data set is selected to contain equal quantities of data collected with each magnetic field polarity. Events are randomly removed from the largest subsample of the two magnetic field polarity configurations.

Each data sample is investigated for background contamination. The reconstructed  $D^0$  mass is searched for evidence of backgrounds from misreconstructed  $D^0$  decays in which  $K/\pi$  misidentification has occurred. Candidates in which only a single final-state particle is misidentified are reconstructed outside the  $m(hhhh)$  signal range. No evidence for candidates with two, three, or four  $K/\pi$  misidentifications is observed. Charm mesons from  $b$ -hadron decays are strongly suppressed by the requirement that the  $D^0$  candidate originates from a primary vertex. This source of background is found to have a negligible contribution.

## 4 Method

Figure 1 shows the  $m(hhhh)$  and  $\Delta m$  distributions for  $D^0$  candidate decays to the final states  $K^-K^+\pi^-\pi^+$ ,  $\pi^-\pi^+\pi^+\pi^-$ , and  $K^-\pi^+\pi^+\pi^-$ , for data taken with magnet up polarity. The distributions for  $\bar{D}^0$  candidates and data taken with magnet down polarity are consistent with the distributions shown. Two-dimensional unbinned likelihood fits are made to the  $m(hhhh)$  and  $\Delta m$  distributions to separate signal and background contributions. Each two-dimensional  $[m(hhhh), \Delta m]$  distribution includes contributions from the following sources: signal  $D^0$  mesons from  $D^{*+}$  decays, which peak in both  $m(hhhh)$  and  $\Delta m$ ; combinatorial background candidates, which do not peak in either  $m(hhhh)$  or  $\Delta m$ ; background candidates from an incorrect association of a soft pion with a real  $D^0$  meson, which peak in  $m(hhhh)$  and not in  $\Delta m$ ; incorrectly reconstructed  $D_s^+ \rightarrow K^-K^+\pi^-\pi^+\pi^+$  decays, which peak at low values of  $m(hhhh)$  but not in  $\Delta m$ ; and misreconstructed  $D^0 \rightarrow K^-\pi^+\pi^-\pi^+\pi^0$  decays, which have broad distributions in both  $m(hhhh)$  and  $\Delta m$ . The signal distribution is described by a Johnson function [18] in  $\Delta m$  and a Crystal Ball function [19] plus a Gaussian function, with a shared peak value, in  $m(hhhh)$ . The combinatorial background is modelled with a first-order polynomial in  $m(hhhh)$ , and the background from  $D^0$  candidates each associated with a random soft pion is modelled by a Gaussian distribution in  $m(hhhh)$ . Both combinatorial and random soft pion backgrounds are modelled with a function of the form

$$f(\Delta m) = [(\Delta m - \Delta m_0) + p_1 (\Delta m - \Delta m_0)^2]^a \quad (2)$$

in  $\Delta m$ , where  $\Delta m_0$  is the kinematic threshold (fixed to the pion mass), and the parameters  $p_1$  and  $a$  are allowed to float.

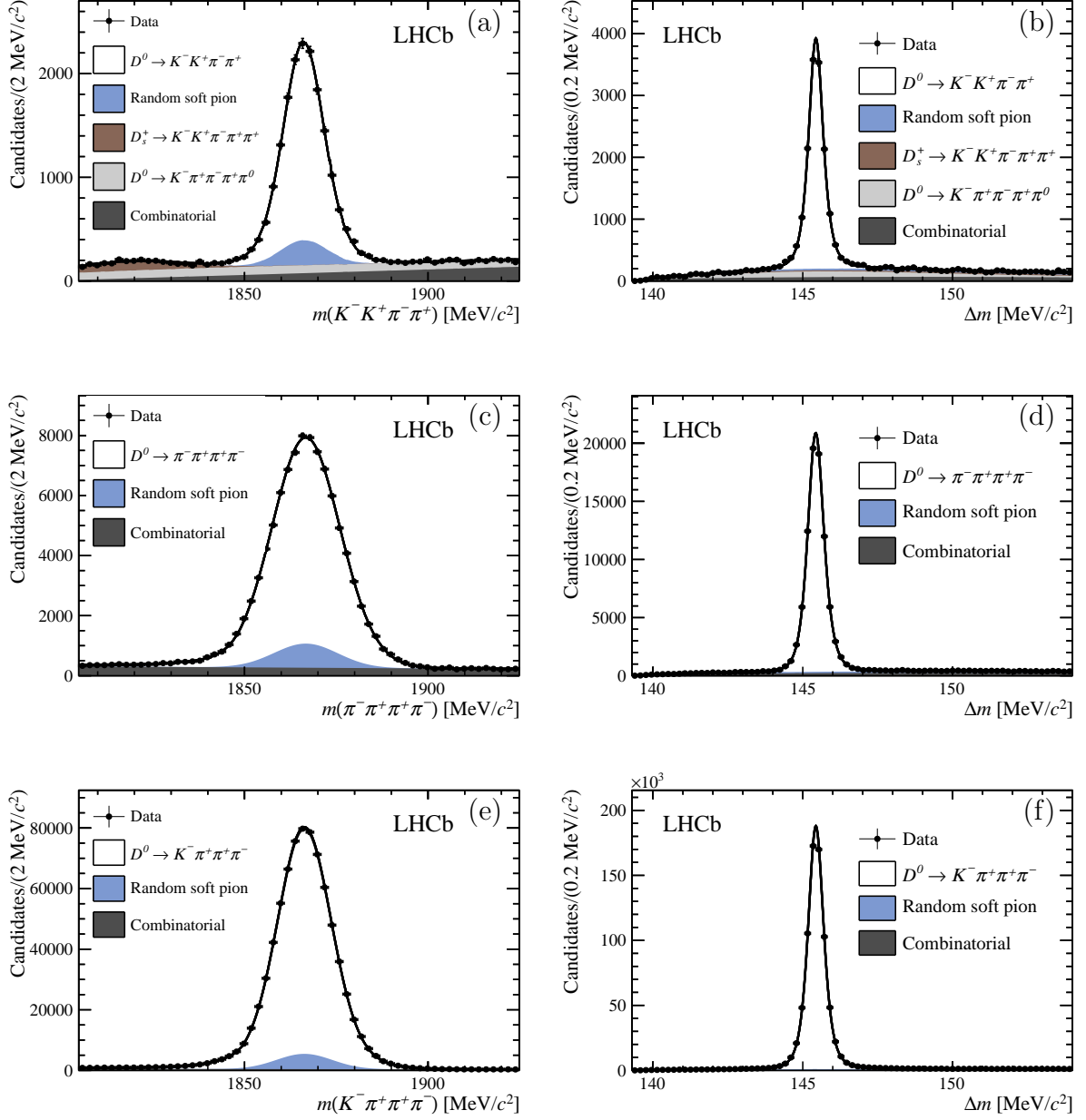


Figure 1: Distributions of (a,c,e)  $m(hhhh)$  and (b,d,f)  $\Delta m$  for (a,b)  $D^0 \rightarrow K^- K^+ \pi^- \pi^+$ , (c,d)  $D^0 \rightarrow \pi^- \pi^+ \pi^+ \pi^-$ , and (e,f)  $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$  candidates for magnet up polarity. Projections of the two-dimensional fits are overlaid, showing the contributions for signal, combinatorial background, and random soft pion background. The contributions from  $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+ \pi^0$  and  $D_s^+ \rightarrow K^- K^+ \pi^- \pi^+ \pi^+$  contamination are also shown for the  $D^0 \rightarrow K^- K^+ \pi^- \pi^+$  sample.

Partially reconstructed  $D_s^+ \rightarrow K^- K^+ \pi^- \pi^+ \pi^+$  decays, where a single pion is not reconstructed, are investigated with simulated decays. This background is modelled with a Gaussian distribution in  $m(hhhh)$  and with a function  $f(\Delta m)$  as defined in Eq. 2. Misreconstructed  $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+ \pi^0$  decays where a single  $K/\pi$  misidentification has occurred and where the  $\pi^0$  is not reconstructed are modelled with a shape from simulated decays. Other potential sources of background are found to be negligible.

For each two-dimensional  $[m(hhhh), \Delta m]$  distribution a fit is first performed to the background region,  $139 < \Delta m < 143 \text{ MeV}/c^2$  or  $149 < \Delta m < 155 \text{ MeV}/c^2$ , to obtain the shapes of the combinatorial and soft pion backgrounds. The  $\Delta m$  components of these shapes are fixed and a two-dimensional fit is subsequently performed simultaneously over four samples ( $D^0$  magnet up,  $\bar{D}^0$  magnet up,  $D^0$  magnet down, and  $\bar{D}^0$  magnet down). The peak positions and widths of the signal shapes and all yields are allowed to vary independently for each sample, whilst all other parameters are shared among the four samples. Signal and background distributions are separated with the *sPlot* statistical method [20]. The data sets contain  $5.7 \times 10^4$   $D^0 \rightarrow K^- K^+ \pi^- \pi^+$ ,  $3.3 \times 10^5$   $D^0 \rightarrow \pi^- \pi^+ \pi^+ \pi^-$ , and  $2.9 \times 10^6$   $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$  signal decays.

The phase space of a spin-0 decay to four pseudoscalars can be described with five invariant mass-squared combinations:  $s(1,2)$ ,  $s(2,3)$ ,  $s(1,2,3)$ ,  $s(2,3,4)$ , and  $s(3,4)$ , where the indices 1, 2, 3, and 4 correspond to the decay products of the  $D^0$  meson following the ordering of the decay definitions. The ordering of identical final-state particles is randomised.

The rich amplitude structures are visible in the invariant mass-squared distributions for  $D^0$  and  $\bar{D}^0$  decays to the final states  $K^- K^+ \pi^- \pi^+$  and  $\pi^- \pi^+ \pi^+ \pi^-$ , shown in Figs. 2 and 3, respectively. The momenta of the final-state particles are calculated with the decay vertex of the  $D^*$  constrained to coincide with the primary vertex and the mass of the  $D^0$  candidates constrained to the world average value of  $1864.86 \text{ MeV}/c^2$  [22].

An adaptive binning algorithm is devised to partition the phase space of the decay into five-dimensional hypercubes. The bins are defined such that each contains a similar number of candidates, resulting in fine bins around resonances and coarse bins across sparsely populated regions of phase space.

For each phase-space bin,  $S_{CP}^i$ , defined in Eq. 1, is calculated. The number of signal events in bin  $i$ ,  $N_i$ , is calculated as the sum of the signal weights in bin  $i$  and  $\sigma_i^2$  is the sum of the squared weights. The normalisation factor,  $\alpha$ , is calculated as the ratio of the sum of the weights for  $D^0$  candidates and the sum of the weights for  $\bar{D}^0$  candidates and is  $1.001 \pm 0.008$ ,  $0.996 \pm 0.003$ , and  $0.998 \pm 0.001$  for the final states  $K^- K^+ \pi^- \pi^+$ ,  $\pi^- \pi^+ \pi^+ \pi^-$ , and  $K^- \pi^+ \pi^+ \pi^-$ , respectively.

## 5 Production and instrumental asymmetries

Checks for remaining production or reconstruction asymmetries are carried out by comparing the phase-space distributions from a variety of data sets designed to test particle/antiparticle detection asymmetries and “left/right” detection asymmetries. The “left”

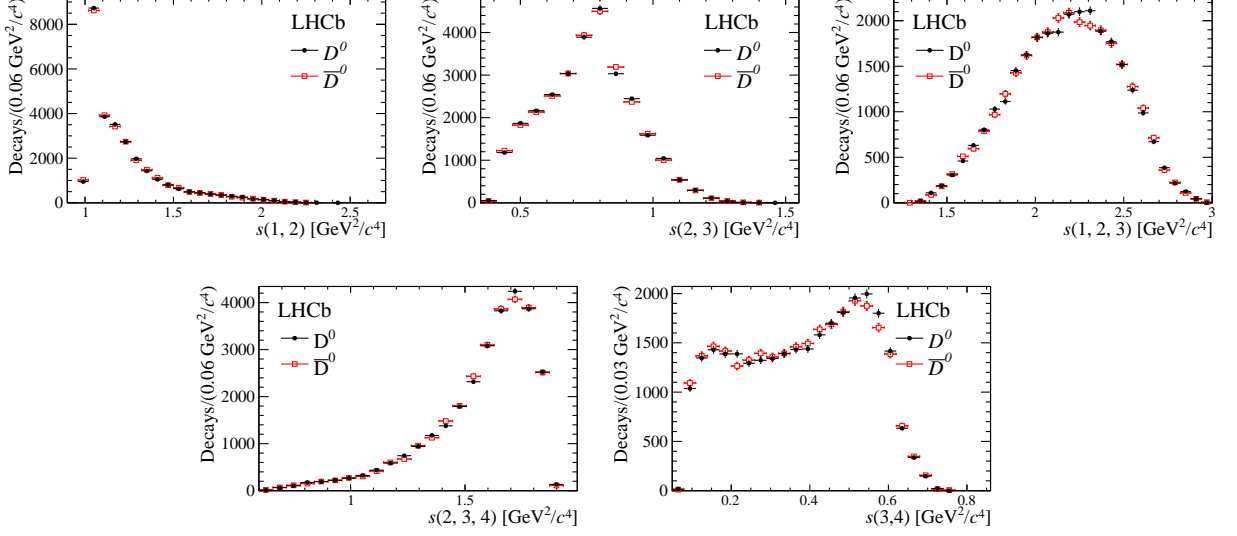


Figure 2: Invariant mass-squared distributions for  $D^0$  meson (black, closed circles) and  $\bar{D}^0$  meson (red, open squares) decays to the final state  $K^- K^+ \pi^- \pi^+$ . The invariant mass-squared combinations  $s(1,2)$ ,  $s(2,3)$ ,  $s(1,2,3)$ ,  $s(2,3,4)$ , and  $s(3,4)$  correspond to  $s(K^-, K^+)$ ,  $s(K^+, \pi^-)$ ,  $s(K^-, K^+, \pi^-)$ ,  $s(K^+, \pi^-, \pi^+)$ , and  $s(\pi^-, \pi^+)$ , respectively for the  $D^0$  mode. The charge conjugate is taken for the  $\bar{D}^0$  mode. The phase-space distribution of the  $D^0 \rightarrow K^- K^+ \pi^- \pi^+$  decay is expected to be dominated by the quasi-two-body decay  $D^0 \rightarrow \phi \rho^0$  with additional contributions from  $D^0 \rightarrow K_1(1270)^\pm K^\mp$  and  $D^0 \rightarrow K^*(1410)^\pm K^\mp$  decays [10].

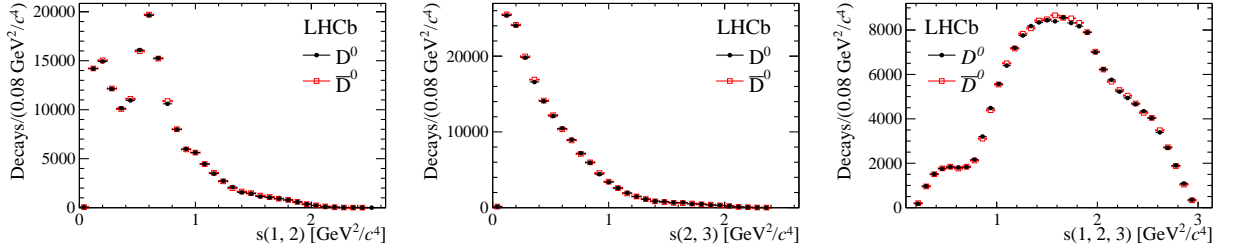


Figure 3: Invariant mass-squared distributions for  $D^0$  meson (black, closed circles) and  $\bar{D}^0$  meson (red, open squares) decays to the final state  $\pi^- \pi^+ \pi^- \pi^-$ . The invariant mass-squared combinations  $s(1,2)$ ,  $s(2,3)$ ,  $s(1,2,3)$ ,  $s(2,3,4)$ , and  $s(3,4)$  correspond to  $s(\pi^-, \pi^+)$ ,  $s(\pi^+, \pi^-)$ ,  $s(\pi^-, \pi^+, \pi^-)$ ,  $s(\pi^+, \pi^+, \pi^-)$ , and  $s(\pi^+, \pi^-)$ , respectively for the  $D^0$  mode. The charge conjugate is taken for the  $\bar{D}^0$  mode. Owing to the randomisation of the order of identical final-state particles the invariant mass-squared distributions  $s(2,3,4)$  and  $s(3,4)$  are statistically compatible with the invariant mass-squared distributions  $s(1,2,3)$  and  $s(1,2)$ , respectively. As such the invariant mass-squared distributions  $s(2,3,4)$  and  $s(3,4)$  are not shown. The phase-space distribution of the  $D^0 \rightarrow \pi^- \pi^+ \pi^- \pi^-$  decay is expected to be dominated by contributions from  $D^0 \rightarrow a_1(1260)^+ \pi^-$  and  $D^0 \rightarrow \rho^0 \rho^0$  decays [21].

direction is defined as the bending direction of a positively charged particle with the magnet up polarity. Asymmetries in the background are studied with weighted background candidates and mass sidebands.

Left/right asymmetries in detection efficiencies are investigated by comparing the phase-space distributions of  $D^0$  candidates in data taken with opposite magnet polarities, thus investigating the same flavour particles in opposite sides of the detector. Particle/antiparticle asymmetries are studied with the control channel  $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$ . The weighting based on  $p_T$  and pseudorapidity of the  $D^0$  candidate and the normalisation across the phase space of the  $D^0$  decay cancel the  $K^+/K^-$  detection asymmetry in this control channel. The phase-space distribution of  $D^0$  decays from data taken with one magnet polarity is compared with that of  $\bar{D}^0$  decays from data taken with the opposite magnet polarity, for any sources of particle/antiparticle detection asymmetry, localised across the phase space of the  $D^0$  decay.

The weighted distributions for each of the background components in the two-dimensional fits are investigated for asymmetries in  $D^0 \rightarrow K^- K^+ \pi^- \pi^+$ ,  $D^0 \rightarrow \pi^- \pi^+ \pi^+ \pi^-$ , and  $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$  candidates. The  $\Delta m$  and  $m(hhhh)$  sidebands are also investigated to identify sources of asymmetry.

The sensitivity to asymmetries is limited by the sample size, so  $S_{CP}$  is calculated only with statistical uncertainties.

## 6 Sensitivity studies

Pseudo-experiments are carried out to investigate the dependence of the sensitivity on the number of bins. Each pseudo-experiment is generated with a sample size comparable to that available in data.

Decays are generated with MINT, a software package for amplitude analysis of multi-body decays that has also been used by the CLEO collaboration [10]. A sample of  $D^0 \rightarrow K^- K^+ \pi^- \pi^+$  decays is generated according to the amplitude model reported by CLEO [10], and  $D^0 \rightarrow \pi^- \pi^+ \pi^+ \pi^-$  decays are generated according to the amplitude model from the FOCUS collaboration [21]. Phase and magnitude differences between  $D^0$  and  $\bar{D}^0$  decays are introduced. Figure 4 shows the  $S_{CP}$  distributions for a typical pseudo-experiment in which no CPV is present and for a typical pseudo-experiment with a phase difference of  $10^\circ$  between  $D^0 \rightarrow a_1(1260)^+ \pi^-$  and  $\bar{D}^0 \rightarrow a_1(1260)^- \pi^+$  decays.

Based on the results of the sensitivity study, a partition with 32 bins, with approximately 1800 signal events, is chosen for  $D^0 \rightarrow K^- K^+ \pi^- \pi^+$  decays while a partition with 128 bins, with approximately 2500 signal events is chosen for  $D^0 \rightarrow \pi^- \pi^+ \pi^+ \pi^-$  decays. The  $p$ -values for the pseudo-experiments are uniformly distributed for the case of no CPV. The average  $p$ -value for a pseudo-experiment with a phase difference of  $10^\circ$  or a magnitude difference of 10% between  $D^0 \rightarrow \phi \rho^0$  and  $\bar{D}^0 \rightarrow \phi \rho^0$  decays for the  $D^0 \rightarrow K^- K^+ \pi^- \pi^+$  mode and between  $D^0 \rightarrow a_1(1260)^+ \pi^-$  and  $\bar{D}^0 \rightarrow a_1(1260)^- \pi^+$  decays for the  $D^0 \rightarrow \pi^- \pi^+ \pi^+ \pi^-$  mode is below  $10^{-3}$ .

## 7 Results

Asymmetries are searched for in the  $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$  control channel. The distributions of  $S_{CP}$  and local  $CP$  asymmetry, defined as

$$A_{CP}^i = \frac{N_i(D^0) - \alpha N_i(\bar{D}^0)}{N_i(D^0) + \alpha N_i(\bar{D}^0)},$$

are shown in Fig. 5 for the  $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$  control channel. The data set is also studied to identify sources of asymmetry with two alternative partitions and by separating data taken with each magnet polarity. The results, displayed in Table 1, show that no asymmetry is observed in  $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$  decays. Furthermore, the data sample is split into 10 time-ordered samples of approximately equal size, for each polarity. The  $p$ -values under the hypothesis of no asymmetry are uniformly distributed across the data taking period. No evidence for a significant asymmetry in any bin is found.

The  $S_{CP}$  and local  $CP$  asymmetry distributions for  $D^0 \rightarrow K^- K^+ \pi^- \pi^+$  decays for a partition containing 32 bins and for  $D^0 \rightarrow \pi^- \pi^+ \pi^+ \pi^-$  decays with a partition containing 128 bins are shown in Fig. 5. The  $p$ -values under the hypothesis of no  $CP$  violation for the decays  $D^0 \rightarrow K^- K^+ \pi^- \pi^+$  and  $D^0 \rightarrow \pi^- \pi^+ \pi^+ \pi^-$  are 9.1% and 41%, respectively. The consistency of the results is checked with alternative partitions and the  $p$ -values are displayed in Table 2.

The stability of the results is checked for each polarity in 10 approximately equal-sized, time-ordered data samples. The  $p$ -values are uniformly distributed across the 2011 data taking period and are consistent with the no CPV hypothesis.

## 8 Conclusions

A model-independent search for CPV in  $5.7 \times 10^4$   $D^0 \rightarrow K^- K^+ \pi^- \pi^+$  decays and  $3.3 \times 10^5$   $D^0 \rightarrow \pi^- \pi^+ \pi^+ \pi^-$  decays is presented. The analysis is sensitive to CPV that would arise from a phase difference of  $\mathcal{O}(10^\circ)$  or a magnitude difference of  $\mathcal{O}(10\%)$  between  $D^0 \rightarrow \phi \rho^0$  and  $\bar{D}^0 \rightarrow \phi \rho^0$  decays for the  $D^0 \rightarrow K^- K^+ \pi^- \pi^+$  mode and between  $D^0 \rightarrow a_1(1260)^+ \pi^-$  and  $\bar{D}^0 \rightarrow a_1(1260)^- \pi^+$  decays for the  $D^0 \rightarrow \pi^- \pi^+ \pi^+ \pi^-$  mode. For none of the 32 bins, each with approximately 1800 signal events, is an asymmetry greater than 6.5% observed for  $D^0 \rightarrow K^- K^+ \pi^- \pi^+$  decays, and for none of the 128 bins, each with approximately 2500 signal events, is an asymmetry greater than 5.5% observed for  $D^0 \rightarrow \pi^- \pi^+ \pi^+ \pi^-$  decays. Assuming  $CP$  conservation, the probabilities to observe local asymmetries across the phase-space of the  $D^0$  meson decay as large or larger than those in data for the decays  $D^0 \rightarrow K^- K^+ \pi^- \pi^+$  and  $D^0 \rightarrow \pi^- \pi^+ \pi^+ \pi^-$  are 9.1% and 41%, respectively. All results are consistent with  $CP$  conservation at the current sensitivity.



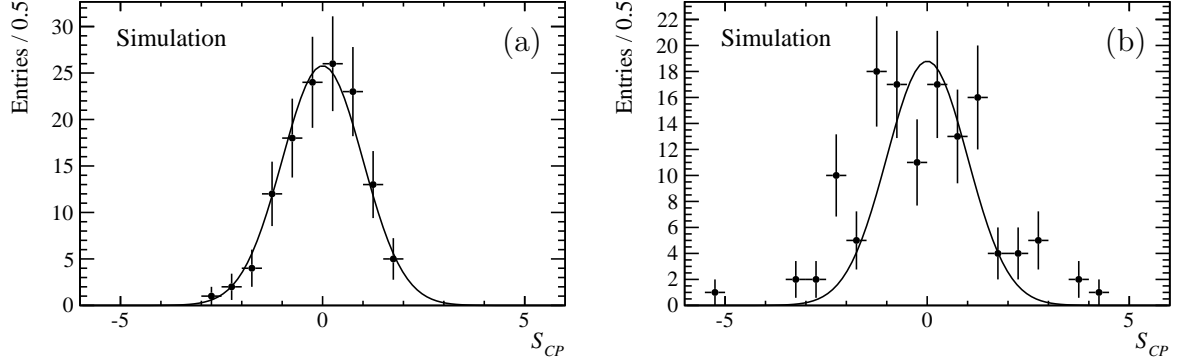


Figure 4: Distributions of  $S_{CP}$  for (a) a typical pseudo-experiment with generated  $D^0 \rightarrow \pi^- \pi^+ \pi^+ \pi^-$  decays without CPV and for (b) a typical pseudo-experiment with a generated  $10^\circ$  phase difference between  $D^0 \rightarrow a_1(1260)^+ \pi^-$  and  $\bar{D}^0 \rightarrow a_1(1260)^- \pi^+$  resonant decays. The points show the data distribution and the solid line is a reference Gaussian distribution corresponding to the no CPV hypothesis. The corresponding  $p$ -values under the hypothesis of no asymmetry for (a) decays without CPV and (b) decays with a  $10^\circ$  phase difference between  $D^0 \rightarrow a_1(1260)^+ \pi^-$  and  $\bar{D}^0 \rightarrow a_1(1260)^- \pi^+$  resonant components are 85.6% and  $1.1 \times 10^{-16}$ , respectively.

Table 1: The  $\chi^2/\text{ndf}$  and  $p$ -values under the hypothesis of no CPV for the control channel  $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$ . The  $p$ -values are calculated separately for data samples taken with magnet up polarity, magnet down polarity, and the two polarities combined.

	$p$ -value (%) ( $\chi^2/\text{ndf}$ )	$p$ -value (%) ( $\chi^2/\text{ndf}$ )	$p$ -value (%) ( $\chi^2/\text{ndf}$ )
Bins	Magnet down	Magnet up	Combined sample
16	80.8 (10.2/15)	21.2 (19.1/15)	34.8 (16.5/15)
128	62.0 (121.5/127)	75.9 (115.5/127)	80.0 (113.4/127)
1024	27.5 (1049.6/1023)	9.9 (1081.6/1023)	22.1 (1057.5/1023)

Table 2: The  $\chi^2/\text{ndf}$  and  $p$ -values under the hypothesis of no CPV with three different partitions for  $D^0 \rightarrow K^- K^+ \pi^- \pi^+$  decays and  $D^0 \rightarrow \pi^- \pi^+ \pi^+ \pi^-$  decays. The  $p$ -values are calculated for a combined data sample with both data taken with magnet up polarity and data taken with magnet down polarity.

$D^0 \rightarrow K^- K^+ \pi^- \pi^+$			$D^0 \rightarrow \pi^- \pi^+ \pi^+ \pi^-$		
Bins	$p$ -value (%)	$\chi^2/\text{ndf}$	Bins	$p$ -value (%)	$\chi^2/\text{ndf}$
16	9.1	22.7/15	64	28.8	68.8/63
32	9.1	42.0/31	128	41.0	130.0/127
64	13.1	75.7/63	256	61.7	247.7/255

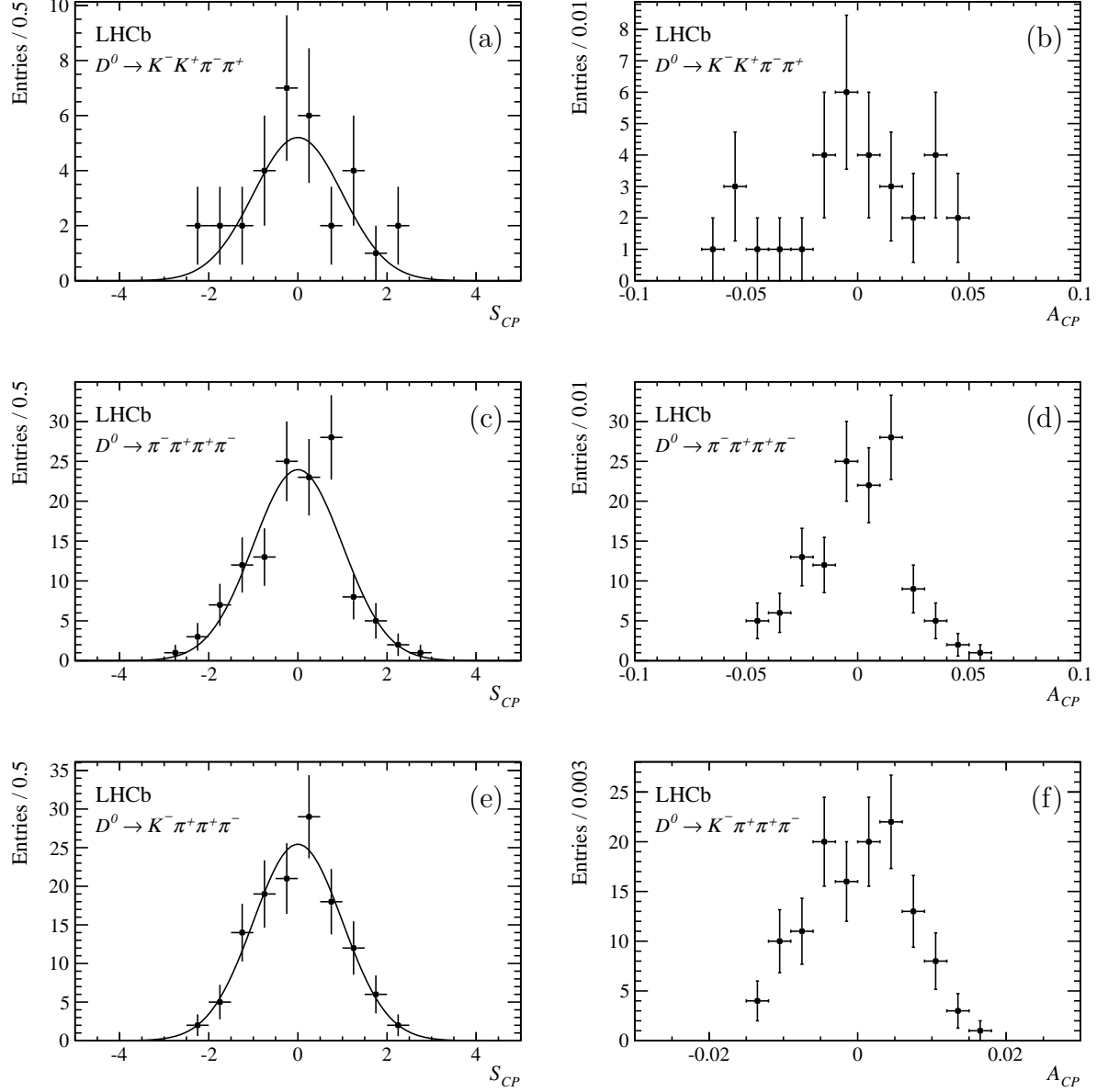


Figure 5: Distributions of (a,c,e)  $S_{CP}$  and (b,d,f) local  $CP$  asymmetry per bin for (a,b)  $D^0 \rightarrow K^- K^+ \pi^- \pi^+$  decays partitioned with 32 bins, for (c,d)  $D^0 \rightarrow \pi^- \pi^+ \pi^+ \pi^-$  decays partitioned with 128 bins, and for (e,f) the control channel  $D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$  partitioned with 128 bins. The points show the data distribution and the solid line is a reference Gaussian distribution corresponding to the no CPV hypothesis.

## Acknowledgements

We express our gratitude to our colleagues in the CERN accelerator departments for the excellent performance of the LHC. We thank the technical and administrative staff at the LHCb institutes. We acknowledge support from CERN and from the national agencies: CAPES, CNPq, FAPERJ and FINEP (Brazil); NSFC (China); CNRS/IN2P3 and Region Auvergne (France); BMBF, DFG, HGF and MPG (Germany); SFI (Ireland); INFN (Italy); FOM and NWO (The Netherlands); SCSR (Poland); MEN/IFA (Romania); MinES, Rosatom, RFBR and NRC “Kurchatov Institute” (Russia); MinECo, XuntaGal and GENCAT (Spain); SNSF and SER (Switzerland); NAS Ukraine (Ukraine); STFC (United Kingdom); NSF (USA). We also acknowledge the support received from the ERC under FP7. The Tier1 computing centres are supported by IN2P3 (France), KIT and BMBF (Germany), INFN (Italy), NWO and SURF (The Netherlands), PIC (Spain), GridPP (United Kingdom). We are thankful for the computing resources put at our disposal by Yandex LLC (Russia), as well as to the communities behind the multiple open source software packages that we depend on.

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